On Popularity Prediction of Videos Shared in Online Social Networks

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ABSTRACT
Popularity prediction, with both technological and economic importance, has been extensively studied for conventional video sharing sites (VSSes), where the videos are mainly found via searching, browsing, or related links. Recent statistics however suggest that online social network (OSN) users regularly share video contents from VSSes, which has contributed to a significant portion of the accesses; yet the popularity prediction in this new context remains largely unexplored. In this paper, we present an initial study on the popularity prediction of videos propagated in OSNs along friendship links.

We conduct a large-scale measurement and analysis of viewing patterns of videos shared in one of largest OSNs in China, and examine the performance of typical views-based prediction models. We find that they are generally ineffective, if not totally fail, especially when predicting the early peaks and later bursts of accesses, which are common during video propagations in OSNs. To overcome these limits, we track the propagation process of videos shared in a Facebook-like OSN in China, and analyze the user viewing and sharing behaviors. We accordingly develop a novel propagation-based video popularity prediction solution, namely SoVP. Instead of relying solely on the early views for prediction, SoVP considers both the intrinsic attractiveness of a video and the influence from the underlying propagation structure. The effectiveness of SoVP, particularly for predicting the peaks and bursts, have been validated through our trace-driven experiments.

Categories and Subject Descriptors
J.4 [Social and Behavioral Sciences]: Sociology; H.3.5 [Information Storage and Retrieval]: Online Information Services—Web-based services

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http://--enter the whole DOI string from rightsreview form confirmation.

General Terms
Measurement, Model

Keywords
Social network, video sharing, popularity prediction, propagation

1. INTRODUCTION
In the past decade, online social networks (OSNs) (e.g., Facebook, Twitter, Google+, and etc.) have become popular online destinations for connecting friends as well as sharing contents. Traditionally, a user finds videos by browsing the front pages or related video lists in such video sharing sites (VSSes) as YouTube, or via search engines [38]. The emergence of OSNs however has greatly changed such access patterns through proactively and efficiently sharing among friends the video links from external VSSes [24]. The latest statistics by YouTube indicate that 500 years of YouTube video are watched every day by Facebook users, and over 700 YouTube videos are shared on Twitter each minute nowadays [36]. The comScore’s statistics [6] in August 2012 further reveal that Facebook has ranked eighth in terms of video content views. Besides Facebook and Twitter, we have seen similar trend around the world. For example, as of May 2011, more than 54 million unique RenRen (the largest Facebook-like OSN in China) users have participated in video viewing and 20 million participated in sharing, generating 12.4 million views, and 1.64 million shares every day [17].

Content providers, advertisers, and Web hosts all expect to predict how many view accesses the individual videos might generate to a given site. For advertising, the popularity count is tied directly with the ad revenue (see for example the ads shown with YouTube videos); an accurate population prediction thus offers a good revenue (or cost) indication for both YouTube and its content generators. For content-distribution networks, the computation, storage, and bandwidth resources can be well planned with a good prediction of the access patterns [31, 18]. There have been extensive studies on popularity prediction for conventional VSSes, mostly leveraging earlier views of a video as the key predictor [30, 21, 9, 26, 34].

1www.renren.com
Although the videos shared in OSNs are generally hosted by VSSes, an OSN proactively spreads videos among its users along friendship relations. As such, a video’s views are not only determined by the users’ interest in it, but also the underlying propagation structure, which generates unique request patterns than that in VSSes. It has been found that the propagation-based video spreading mechanism generates distinguished video popularity distribution [17]. We further find that it would lead to high video popularity dynamics due to great difference of the numbers of users’ friends. As such, even though it is proved that the conventional prediction models perform well in predicting video views in VSSes [30], it is necessary to evaluate their effectiveness in the OSN context and if needed, to develop new tools.

In this paper, we conduct an initial study on the popularity prediction of videos shared in OSNs. Collaborated with a large Facebook-like OSN in China, we first measure and analyze the characteristics of video popularity evolutions in this large OSN. We then test the performance of conventional views-based prediction models, and also propose a novel propagation-based prediction solution. Our contributions are summarized as follows:

- By analyzing long-term traces of video views, we find that video popularity evolution in the OSN is highly dynamic, where the correlations between the views in early and later times are noticeably lower than that in VSSes. The lower correlations pose significant challenges to views based prediction tools.
- We test the performances of the conventional prediction tools including Autoregressive Integrated Moving Average (ARIMA) model, Multiple Linear Regression (MLR), and k-Nearest Neighbors (kNN). These models only need the number of early views as the input, and can be easily developed by VSSes without assistance of OSNs. We find that they are generally ineffective, if not totally fail, especially when predicting the early peaks and later bursts of accesses, which are common during video propagations in OSNs.
- We present a novel propagation-based prediction tool, namely SoVP (Social network assisted Video Prediction). SoVP considers both the intrinsic attractiveness of a video and the influence from the underlying propagation structure. The effectiveness of SoVP, particularly for predicting the request bursts, has been validated through our trace-driven experiments.

The rest of the paper is organized as follows. We introduce some related work in Section 2. Section 3 introduces measurement methodology and depicts the characteristics of video popularity evolution in the OSN. Section 4 introduces the premier knowledge of three conventional views-based prediction models. We propose a novel propagation-based prediction framework in Section 5. Section 6 presents trace-based evaluations. We conclude in Section 7.

2. RELATED WORK

Popularity prediction of online content has been widely studied in the literature. Earlier studies have focused on predicting the spread of information based on time series. Typical solutions include time series models like ARIMA [21, 9], regression models [32, 13, 25, 30, 34, 35], and classification models [32, 26, 27]. For video prediction, they predicted the future views solely based on the early views, which we refer to as views-based predictions. Their efficiency highly depends on the characteristic of the data set. Cha et al. [2] found that, in YouTube, a high linear correlation existed between the number of video views on early days and later days (e.g., correlation coefficient is 0.84 between the 2<sup>nd</sup> day and the 90<sup>th</sup> day). Szabo et al. [30] also found similar results and presented three models using linear correlation and regression for prediction. These models can predict video popularity 30 days ahead with a remarkable accuracy (e.g., relative error of 10%) based on 10-day historic video views. Pinto et al. [22] proposed two models for predicting the future popularity of the YouTube video by learning its early view patterns. In this paper, we study the video accesses through OSN sharing, which is quite different from the conventional YouTube-like accesses [17, 16]; we have examined whether the above conventional models can well predict popularity in this new context and the results are largely negative.

Recently there have been pioneering data-driven analysis of information propagation in different kinds of OSNs, e.g., photos propagation in Flickr network [3], likes and fans pages in Facebook [1, 29, 33], links and retweets in Twitter [11, 24, 4, 8, 14, 19, 37], and voting in Digg [14, 28, 15]. There have also been efforts towards prediction in this context [8, 11, 15]. Galuba et al. [8] proposed a propagation model that predicts which users are likely to mention which URLs in Twitter. Hong et al. [11] treated the retweets prediction in Twitter as a classification task. They investigated a wide spectrum of features to determine which ones can be successfully used as predictors of popularity. Kooti et al. [12] investigated the prediction of emerging social conventions on Twitter. The most close research to ours was conducted by Lerman et al. [15]. They predicted popularity of news in Digg, by incorporating aspects of the web site design. They showed that their model-based prediction improves prediction based on simply extrapolating from the early votes. Our work has been inspired by these studies, and differs from theirs in that we focus on video, which, as one of the most information-rich data objects, preserves unique characteristics that are yet to be examined for prediction.

3. VIDEO PROPAGATION AND POPULARITY EVOLUTION

This section introduces our measurement methodology, and depicts the characteristics of video propagation and popularity evolution in the OSN.

3.1 Measurement Methodology

To understand video spreading in OSNs, we closely collaborate with a large-scale Facebook-like OSN in China to collect and analyze its video-related user behaviors. Like Facebook, its users primarily interact with information through an aggregated history of their friends’ recent activity, called the “News Feed”. For video sharing, typically a user may post a video link from a VSS, and the link will appear in its friends’ “News Feed”. Some friends may click and view the video, and such viewers can then decide whether to share the video. If they click the “share” button, the video...
link will appear in their friends’ “News Feed” and hence the video can further propagate.

1. User A posted a video \( x \) at time \( T_0 \);
   \( (T_0, V_x, U_A, U_A, U_A) \) to log server

2. User B viewed \( V_x \) shared by \( U_A \) at time \( T_1 \);
   \( (T_1, V_x, U_B, U_A, U_A) \) to log server

3. User C viewed \( V_x \) shared by \( U_B \) at time \( T_2 \);
   \( (T_2, V_x, U_C, U_B, U_A) \) to log server

**Figure 1: Illustration of video propagation and corresponding logs**

The data collection process works as follows: when a user clicks a video link shared by her/his friend, a record will be sent to a log server; and the data format is: \( (\text{Starting Time}, \text{Video URL}, \text{Viewer ID}, \text{Direct Sharer ID}, \text{Initial Sharer ID}) \).

We use an example in Fig. 1 to illustrate the video propagation and the corresponding log record. Initially at time \( T_0 \), user \( A \) (denoted as \( U_A \)) posted video \( x \) (denoted as \( V_x \)) from a VSS, and then a record \( (T_0, V_x, U_A, U_A, U_A) \) is sent to log server. Since \( U_A \) is the initial user, both direct sharer and initial sharer are itself; At time \( T_1 \), user \( B \) viewed \( V_x \) through the share link created by \( U_A \), and then \( U_B \) further shared \( V_x \) after watching it; and then a record \( (T_1, V_x, U_B, U_A, U_A) \) is sent to log server. Also as \( U_A \) is the initial user, the initial sharer is \( U_A \); At the Time \( T_2 \), user \( C \) viewed \( V_x \) through the share link created by \( U_B \). A new record \( (T_2, V_x, U_C, U_B, U_A) \) is sent to log server. Note that there is a dotted line without any arrow between the friends \( U_A \) and \( U_C \), which means although \( U_A \)’s shared video was exposed in \( U_C \)’s “News Feed”, \( U_C \) did not click it maybe because s/he is offline.

**Table 1: Summary of trace in one-day period**

<table>
<thead>
<tr>
<th>Views</th>
<th>Shares</th>
<th>Users</th>
<th>Videos</th>
<th>New Videos</th>
</tr>
</thead>
<tbody>
<tr>
<td>12,432,708</td>
<td>1,628,852</td>
<td>3,514,461</td>
<td>201,517</td>
<td>71,236</td>
</tr>
</tbody>
</table>

Using (Video URL, Viewer ID), we can extract the number of views of any video in each day. We then use this information to analyze the video popularity evolution patterns, and test views-based prediction models. Using (Video URL, Viewer ID, Direct Sharer ID), we can examine the share-view relationship between two friends. And together with the initial Sharer ID, we can restore a video’s propagation process. Such information is useful to analyze the reason underlying the popularity evolution patterns, and inspire the design of our propagation-based prediction model. Our study in this paper is based on a one-month trace that began from March 24th, 2011, since we find that most requests of a video are generally cumulated in the first month, and after that the daily requests decline to a very small scale. Table 1 presents the statistics in a typical one-day period (March 24th, 2011) during the measurement. Our records covered all video requests in the measurement period. In the one-month period, we recorded about 370 million views and 49 million shares.

**3.2 Video Propagation**

A common video propagation process is like this: Initially, a user shares a video link to an OSN directly from a VSS. Immediately, this user’s friends can find this video in their “News Feed”, and some of them watch this video. After that, some portion of these viewers will share this video and can recommend it to their friends. To specify this process, we give the following definitions. We call the users in the root of a propagation tree initiators. These users are the ones who independently shared the video directly from VSSes. We call the users who re-shared the video spreaders. We call the users who watched the shared video viewers. Since spreaders generally watched the video before re-shared it, most of them are also viewers. The definition of viewers is different from that in [12, 20]. In their model, the viewers are exclusive of spreaders. We define a video’s popularity as the number of its viewers. We define the Branching Factor (BrF) as the number of viewers directly follow a spreader. We define the ShareRate (ShR) as the ratio of the viewers that re-share the video after watching it.

**Figure 2: Illustration of a video propagation**

The video propagation of popular videos are very complex. For example, we find one video which consists of 1022 initiators, 153185 spreaders, and 995707 viewers over one month propagation. Each of 1022 propagation trees exhibits unique patterns. We choose two among them and illustrate their propagation structures over several hours in Fig. 2. Each vertex is a user and the arrows means that a user has viewed the video shared by his/her friend. We can observe some super spreaders in the left tree, who are followed by hundreds of viewers, while the spreaders in the right tree attract moderate viewers. The two different trees from the same video gives us an illustration that the underlying OSN topology plays a foundational role in video propagation and popularity evolution.

**3.3 Popularity Evolutions of Typical Videos**

According to a video’s attractiveness (ShR and BrF), we roughly classify popular videos into three types: high BrF & high ShR, high BrF & low ShR, and low BrF & high ShR. Although finer classifications like the work in [7] would be possible and worth further study, current classification is enough to explore the limits of conventional models in predicting popularity of videos shared in OSNs.

3\Since the paper concentrates on popular videos, the category low BrF & low ShR is not mentioned, which generally refers to unpopular videos (e.g., less than 10 views per day).
3.4 Correlation between Early and Later Views

We choose one typical video from each type and show them in Fig. 3, 4 and 5, respectively. The middle and lower sub-figures show the evolution of ShR and BrF. The upper sub-figures show the evolution of video views in each day. The type-1 video was the most popular video in our sample videos. It kept the views at a very high level during the first week. Although experiencing decreasing views after that, it still received more than seven thousands views after one month. Like the type-1 video, the type-2 video also experienced a surge-growth over first few days (e.g., two days), acquiring huge (e.g., 90%) views. Yet different from the type-1 video, it quickly turned to the sluggish state after the peak, only receiving less than a hundred of views every day after one week. The type-3 video stayed dormant for several days (e.g., nearly one week) after they were first shared in the OSN; then it experienced a dramatic increase and attracted a large portion of total views within a few days. Overall, while the video shared in OSNs generally experiences a re-quest burst, it is uncertain about the start time, the height and duration of the burst. In the performance evaluation section we will find these uncertainties pose challenges to conventional views-based prediction models.

4. VIEWS-BASED PREDICTION

One target of this paper is to investigate whether the number of future (e.g., one-day ahead) views can be accurately predicted simply based on early views, which can be easily obtained by VSSes so that they can do predictions without assistsances of OSNs. To do this, we will examine three conventional prediction models: ARIMA [21], MLR [25], and kNN [20]. To make predictions, they either utilize the early views of the predicted video itself or utilize the similarity of the popularity evolution pattern with early published videos. Here we provide some primary knowledge of these models, and present their performance in Section 6.

4.1 Autoregressive Integrated Moving Average (ARIMA)

We first examine Autoregressive Integrated Moving Average (ARIMA), one of the most popular time series models for predicting future values of a time series [21, 9]. Given the time series of video popularity in the past several days, it can make fine-grained prediction for the video’s future evolution, leveraging the trend, periodicity and autocorrelation exhibited in the history information. ARIMA consists of three parts: an Autoregressive (AR) model, a Moving Average (MA) model and an integrated part. They are applied in the cases where data show evidence of non-stationarity and an initial differencing step (corresponding to the “inte-
An MA model of order $p$ is defined as:

$$Y(t) = \sum_{i=1}^{p} \beta_i Y(t-i) + \epsilon_t$$

(1)

where $Y(t)$ is the number of views in the $t^{th}$ day; $\beta_1, \ldots, \beta_p$ are the parameters of the model; and $\epsilon$ is a white noise error term.

A major drawback of ARIMA model is that it needs a high correlation of neighbor videos shared by their friends, and etc. Yet, how to utilize such information in video popularity prediction is not easy, as the previous work has shown that they have no simple (e.g., linear) relationship with the video popularity [16]. In this section, we propose a novel propagation-based prediction framework to predict video future views in the OSN.

### 5. PROPAGATION-BASED PREDICTION

Comparing with VSSes, OSNs know much more information about a video beyond the number of its early views, such as viewers, sharers, whether viewers would like to share the video after viewing, whether users would like to view the videos shared by their friends, and etc. Yet, how to utilize such information in video popularity prediction is not easy, as the previous work has shown that they have no simple (e.g., linear) relationship with the video popularity [16].

Before modeling the video propagation, we first define some notations. For a given video, $V(t)$ and $S(t)$ are defined as the sets of its viewers and sharers by the time $t$, respectively. We use $|V(t)|$ to denote the number in the set $V(t)$, and this notation can also apply to other sets such as $S(t)$. $ShR(t)$ (short for Sharing Rate) is the probability that a user will reshare a video after viewing it. $ViR(t)$ (short for Viewing Rate) is the probability that a user will eventually view the video shared by his/her friend. To some extent, both $ShR(t)$ and $ViR(t)$ reflect how interesting the video is. $W(t)$ is the number of sharers’ friends by time $t$ who have not yet viewed the video. In other words, $W(t) = \sum_{i=1}^{t-1} |V_i| - |V(t)|$. Similar to [10], we assume the $W(t)$ users view the video at a constant rate, which is denoted by $\lambda$. $f(S(t))$ is the number of friends of the new sharer exclusive of those friends who viewed the video before the time $t$. Generally, the average new potential viewers brought by per new sharer will decrease as the increase of the number of sharers in $S(t)$, because most of the new sharer’s friends may have already viewed the video from his/her other friends who also shared the video earlier than the new sharer.

Based on the above notations, the propagation process of one video can be described by the following three equations:

$$\frac{d|V(t)|}{dt} = \lambda \cdot W(t)$$

(6)

$$\frac{d|S(t)|}{dt} = ShR(t) \cdot \frac{d|V(t)|}{dt}$$

(7)

$$\frac{dW(t)}{dt} = \frac{d|S(t)|}{dt} \cdot f(S(t)) \cdot ViR(t) - \frac{d|V(t)|}{dt}$$

(8)

where Eq. 6 reflects that the increased viewers during $dt$ come from the potential viewers $W(t)$, who are going to view the video at a rate of $\lambda$. Eq. 7 reflects that $ShR(t)$ portion of new viewers ($d|V(t)|$) can become sharers during $dt$. Based on the previous measurement work [5], here we assume that viewers will immediately share the video after the viewing, otherwise will never share the video. Recalling that we define $W(t) = \sum_{i=1}^{t-1} |V_i| - |V(t)|$. Accordingly, the variation of $W(t)$ during time $dt$ ($dW(t)$) can be expressed as the combination of the growth
in the number of potential viewers brought by new sharers \(d[S(t)] \cdot f(S(t)) \cdot V_iR(t)\) and the reduction caused by the views during \(dt\) \((-d[V(i)])\). This relation is given in Eq. 8.

Initially, there is only one sharer (we call it initiator), who posted the video from a VSS. Thus, \(S(0)=1, V(0)=1,\) and \(W(0)=1\) equal to the number of friends of the initiator multiplying \(V_iR(0)\). There are four parameters that will affect the evolution of \(W(t): ShR, V_iR, f(S(t))\) and \(\lambda\). \(ShR\) and \(V_iR\) reflect the characteristics of specific videos to some extent; \(f(S(t))\) depends on the friends of the sharers and social topology around them; \(\lambda\) depends on the frequencies users visit the OSN and watch videos. Our prediction framework in the following subsections will introduce how these parameters can be extracted from real trace.

For ease of exposition, Table 2 provides a reference for major notations used in this paper. Generally, we use upper superscript \(k\) (e.g., \(k \in V^k\)) to denote a video \(k\), and lower subscript \(i\) (e.g., \(i \in V_i\)) to denote a user \(i\). Note that for concise presentation, sometimes we may omit the video superscripts under the premise of no concept confusion (e.g., use \(V(t)\) to denote \(V^k(t)\) of video \(k\)).

<table>
<thead>
<tr>
<th>Table 2: Summary of major notations</th>
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</thead>
<tbody>
<tr>
<td>Notation</td>
</tr>
<tr>
<td>(F_i)</td>
</tr>
<tr>
<td>(V_{i,j})</td>
</tr>
<tr>
<td>(V_i)</td>
</tr>
<tr>
<td>(S_i)</td>
</tr>
<tr>
<td>(S_{RF})</td>
</tr>
<tr>
<td>(ShR_i)</td>
</tr>
<tr>
<td>(V_iR_{i,j})</td>
</tr>
<tr>
<td>(BrF_i)</td>
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<tr>
<td>(V^k(t))</td>
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<tr>
<td>(S^k(t))</td>
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<tr>
<td>(W^k(t))</td>
</tr>
<tr>
<td>(\alpha^k)</td>
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<tr>
<td>(\beta^k)</td>
</tr>
<tr>
<td>(ShR^k)</td>
</tr>
<tr>
<td>(V_iR^k)</td>
</tr>
<tr>
<td>(ShR^k_i)</td>
</tr>
<tr>
<td>(V_iR_{i,j})</td>
</tr>
<tr>
<td>(t^k)</td>
</tr>
<tr>
<td>(\lambda)</td>
</tr>
<tr>
<td>(\Phi(t))</td>
</tr>
<tr>
<td>(f(S(t)))</td>
</tr>
</tbody>
</table>

5.2 Framework of SoVP

The propagation-based prediction architecture, as shown in Fig. 7, consists of data collection module, graph learning module, video analysis module, and popularity prediction module. First, the data collection module collects logs that record user viewing actions. The basic log format is \((Video ID, Viewer ID, Sharer ID, Time)\), the meaning of which is described in Section 3. Then the logs are taken as the inputs by the graph learning module and the video analysis module. For the graph learning module, historic user viewing records are used as the input. The graph learning module generates a graph called video-active graph, which records the viewing-sharing relationships between users as well as the statistics of user sharing and viewing actions. The video analysis module takes two kind of inputs: video information (sharers \(S^k\) and viewers \(V^k\)) that is got directly from the data collection module, and the video-active graph that is generated by the graph learning module. The video analysis module analyzes video attractiveness (\(\alpha^k, \beta^k\)) in the context of the video-active graph. Finally, the popularity prediction module uses both the video-active graph and the video attractiveness to make predictions.

5.3 Video-active Graph Learning Module

The topology of an OSN is an important influencing factor to the propagation of videos shared in it. Instead of simply using the original unweighed friend-friend graph, we build a weighted graph called video-active graph. There is a directed edge from user \(i\) to user \(j\) if the user \(j\) viewed a video shared by the user \(i\). We assign weights to vertices and edges according to users’ viewing and sharing activity. Users show inhomogeneous activity in sharing and viewing videos. For example, as shown in Fig. 8, the power-law distribution indicates that the numbers of videos viewed by each user in one-month period exhibits large skewness.

| Figure 7: Framework of SoVP |

Fig. 9 illustrates the properties of vertices and edges in the video-active graph. The properties of a vertex \(i\) include a set of viewed videos \(V_i\), a set of shared videos \(S_i\), and sharing rate \((ShR_i)\). The properties of an edge \((i, j)\) include \(V_{i,j}\), which is defined as the set of video viewed by user \(j\) and shared by user \(i\), and \(V_iR_{i,j}\), which is defined as the ratio that user \(j\) has viewed the videos shared by user \(i\). Taking records (Video ID, Viewer ID, Sharer ID) as the input in a chronological order, \(V_i, S_i, V_{i,j}\) can be extracted directly. \(ShR_i\) and \(V_iR_{i,j}\) can thus be calculated by \(ShR_i = \frac{S_i}{V_i}\), and \(V_iR_{i,j} = \frac{|V_{i,j}|}{|S_i|}\), respectively.
For a given video \( k \), the video analysis module calculates two factors (\( \alpha^k(t) \) and \( \beta^k(t) \)) to reflect the normalized video attractiveness. The calculation methods are shown in Eq. 10 and 11, respectively.

\[
\alpha^k(t) = \frac{|V^k(t)|}{\sum_{i \in S^k(t)}(\Phi(t - t^i_j) \cdot \sum_{j \in F_i} ViR_{i \rightarrow j})}
\]

where \( \Phi(t) \) is the cumulative distribution function (CDF) of time span between sharing a video and the actual view of this shared video by the sharer’s friends. We studied the fitting function in the prior work [5]. It is a combined distribution with Weibull (\( t \geq 2100, k = 0.392, \lambda = 1945 \)) and Generalized Pareto (\( x \geq 2100, \mu = -2654, \sigma = 6315, \xi = 0.669 \)) [5]. \( t^i_j \) is the sharing time of video \( k \) by sharer \( j \). \(|V^k(t)|\) is the actual number of cumulated viewers of video \( k \) by time \( t \). \( \sum_{i \in S^k(t)}(\sum_{j \in F_i} (ViR_{i \rightarrow j} \cdot \Phi(t))) \) is the estimated average number of cumulated viewers over all videos. The \( \alpha \) of an attractive video is usually bigger than 1.

\[
\beta^k(t) = \frac{|S^k(t)|}{\sum_{i \in V^k(t)} ShR_i}
\]

where \(|S^k(t)|\) is the actual number of cumulated sharers of video \( k \) by time \( t \). \( \sum_{i \in V^k(t)} ShR_i \) is the estimated average number of cumulated sharers over all videos. The \( \beta \) of an attractive video is usually bigger than 1.

When making predictions, we use Eq. 12 and Eq. 13 to decide whether a user will view or share the video \( k \), respectively. The decisions depend on both the video attractiveness and social context.

\[
ViR_{i \rightarrow j}^k = \alpha^k(t) \cdot ViR_{i \rightarrow j}
\]

\[
ShR_i^k = \beta^k(t) \cdot ShR_i
\]

5.5 Popularity Prediction Module

Based on our propagation model, the popularity prediction module takes the information of both video attractiveness and the video-active graph as the input to make predictions.

We rewrite Eq. 6 as Eq. 14, which calculates the number of video views during the time \( \Delta \) (e.g., one day in this paper). And \( v_\Delta \) is what we finally need to calculate to be as the predicted views during the time \( \Delta \). According to Eq. 14, we need \( W(t) \) to calculate \( v_\Delta \). We can easily calculate the \( W(t) \) at the beginning time of \( \Delta \) by Eq. 15. Then what we also need to do is to infer \( W(t) \) during the time \( \Delta \).

\[
v_\Delta = |V(T + \Delta)| - |V(T)| = \int_T^{T+\Delta} \lambda \cdot W(t) \, dt
\]

\[
W(T) = \sum_{i \in S^k(T)} \sum_{j \in F_i} ViR_{i \rightarrow j}^k - |V(T)|
\]

From Eq. 6, 7, and 8, we get Eq. 16.

\[
\frac{dW(t)}{dt} = \lambda \cdot W(t) \cdot (ShR(t) \cdot ViR(t) \cdot f(S(t)) - 1)
\]
We define $\omega$ as:

$$\omega = \lambda (ShR(t) \cdot f(S(t))) \cdot ViR(t) - 1$$

(17)

Then Eq. 16 can be rewritten as Eq. 18.

$$dW(t) = \omega \cdot W(t)$$

(18)

Since in a short period the users’ interest in a video will not vary a lot, we assume $\omega$ is a constant value from time $T$ to $T + \Delta$, Eq. 18 can be further expressed as Eq. 19.

$$W(t) \approx \delta \cdot e^{\omega t}$$

(19)

where $\delta$ can be calculated using the initial value of $W(t)$ at time $T$, as is shown in Eq. 15.

Finally, from Eq. 14 and 19, we get:

$$v_{\Delta} = |V(T + \Delta)| - |V(T)| \approx \frac{\lambda}{\omega} (e^{\omega(T+\Delta)} - e^{\omega T})$$

(20)

where $T$ and $T + \Delta$ are the beginning time and the end time of the day when we need to predict.

6. PERFORMANCE EVALUATION

In this section we compare the performances of conventional views-based prediction models with our propagation-based prediction model, SoVP. We first examine their overall performance on a large set of popular videos. We further examine their performances on the three typical popular videos, which can provide a direct illustration about what kind of evolutions may make the conventional prediction models inefficient.

6.1 Performance Metrics

We evaluate the efficiency of the prediction models using the metric of Relative Absolute Error (RAE). For the video $k$ on the day $t$, we have:

$$RAE_k(t) = \frac{|\hat{N}_k(t) - N_k(t)|}{N_k(t)}$$

(21)

where $\hat{N}_k(t)$ is the predicted number of views of video $k$ on the day $t$, and $N_k(t)$ is the actual number of views. For the average RAE of all testing videos on the day $t$, we have:

$$RAE(t) = \frac{\sum_k |\hat{N}_k(t) - N_k(t)|}{\sum_k N_k(t)}$$

(22)

For the average RAE of all testing videos on all testing days, we have:

$$RAE = \frac{\sum_t \sum_k |\hat{N}_k(t) - N_k(t)|}{\sum_t \sum_k N_k(t)}$$

(23)

6.2 Prediction Results

As shown in the previous work [17], video popularity distribution exhibits extremely high skewness that top-2% videos account for over 90% views. For the remaining 98% unpopular videos, any of them only received less than 10 views per day on average. Therefore, we take those top-2% popular videos that were initially shared on the same day (March 24th, 2011) as our test set.

First, we need to select proper models for MLR and $k$NN. We split our data set into a training set that contains the viewing information of 27000 videos, and a test set that contains the viewing information of another 5000 videos. For both MLR and $k$NN regression, we vary the value of $n$ from 1 to 9; for $k$NN regression, we also vary the value of $k$ from 1 to 4. We evaluate the performance of each settings on the test data set and the results are shown in Fig. 10 and 11, respectively. Considering the tradeoff of RAE and complexity, we select $n = 5$ for MLR, and $n = 1$ and $k = 3$ for $k$NN.

Then, we evaluate the overall performance of SoVP as well as the three conventional models with the selected parameters. The average RAE over all test videos for each day is shown in Fig 12. Overall, the SoVP has much better prediction performance than other three models. It is worth noting that ARIMA requires several (e.g., 4 in our experiments) days of early views to learn the model, and so its prediction starts from the fifth day. For MLR, $n = 5$ is used starting from the sixth day, and smaller values are used for earlier days (e.g., $n = 1$ for the second day and $n = 2$ for the third day). ARIMA works well in later days, say after 12 days. It can dynamically select the length of historical information used to predict for each day. For MLR, it works better during the first 10 days and its performance is rather stable. $k$NN shows dynamic performance. For some days it has the most accurate prediction while for others it performs much worse. The reason is that only the number of views during the last day is used and the popularity distribution could change significantly day by day.

Table 3: RAE of predictions for the type-1 video

<table>
<thead>
<tr>
<th></th>
<th>day 2</th>
<th>day 3</th>
<th>day 4</th>
<th>day 5</th>
<th>day 6</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k$NN</td>
<td>0.823</td>
<td>0.580</td>
<td>0.765</td>
<td>0.720</td>
<td>0.314</td>
</tr>
<tr>
<td>MLR</td>
<td>0.886</td>
<td>0.952</td>
<td>0.907</td>
<td>0.820</td>
<td>0.742</td>
</tr>
<tr>
<td>SoVP</td>
<td>0.262</td>
<td>0.247</td>
<td>0.186</td>
<td>0.208</td>
<td>0.157</td>
</tr>
</tbody>
</table>

Table 4: RAE of predictions for the type-2 video

<table>
<thead>
<tr>
<th></th>
<th>day 2</th>
<th>day 3</th>
<th>day 4</th>
<th>day 5</th>
<th>day 6</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k$NN</td>
<td>2.729</td>
<td>2.466</td>
<td>1.199</td>
<td>0.212</td>
<td>2.656</td>
</tr>
<tr>
<td>MLR</td>
<td>0.843</td>
<td>0.811</td>
<td>0.664</td>
<td>0.538</td>
<td>0.233</td>
</tr>
<tr>
<td>SoVP</td>
<td>0.179</td>
<td>0.087</td>
<td>0.108</td>
<td>0.129</td>
<td>0.183</td>
</tr>
</tbody>
</table>

Table 5: RAE of predictions for the type-3 video

<table>
<thead>
<tr>
<th></th>
<th>day 26</th>
<th>day 27</th>
<th>day 28</th>
<th>day 29</th>
<th>day 30</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k$NN</td>
<td>0.926</td>
<td>0.920</td>
<td>0.937</td>
<td>0.808</td>
<td>0.932</td>
</tr>
<tr>
<td>MLR</td>
<td>0.951</td>
<td>0.942</td>
<td>0.921</td>
<td>0.832</td>
<td>0.805</td>
</tr>
<tr>
<td>ARIMA</td>
<td>0.826</td>
<td>0.684</td>
<td>0.947</td>
<td>0.631</td>
<td>0.219</td>
</tr>
<tr>
<td>SoVP</td>
<td>0.400</td>
<td>0.525</td>
<td>0.290</td>
<td>0.327</td>
<td>0.429</td>
</tr>
</tbody>
</table>

We also apply prediction models to the three typical videos that are depicted in Section 4. The original daily views as well as the prediction results are shown in Fig. 13, 14, and 15 respectively. Overall, we can see that the predictions of the three conventional models deviate a lot from the real values, while SoVP works much better than other three models, especially when predicting during the request bursting periods. Since views during the short-term bursts usually count
This paper presented an initial study on popularity prediction of videos shared in OSNs. We measured and analyzed the characteristics of video propagation and popularity in a large-scale Facebook-like OSN. The results suggested that the video views in early and later times exhibit much less correlation than that in VSSes, which poses significant challenges on conventional views-based prediction models. Our experiments with such conventional prediction models as ARIMA, MLR, and kNN confirmed their ineffectiveness in this new context, especially when predicting the requests bursts that are common for the evolutions of videos shared in OSNs. To overcome the limits, we developed a dynamic model to analyze the video propagation process, and accordingly presented a propagation-based prediction framework, SoVP. SoVP considers both video attractiveness and social context in predicting future video views, whose accuracy has been demonstrated by our trace-driven experiments.

Although SoVP can generally get better prediction than the conventional views-based prediction models, its complexity and scalability are not as good as them. Therefore, a compromised solution between SoVP and the conventional models may be a better choice, and we will consider it in our future work. For example, one possible solution could be simplifying SoVP by only leveraging recent video propagation information. We could also incorporate the variables used in SoVP into the conventional models.

7. CONCLUSIONS AND FUTURE WORK

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8. ACKNOWLEDGMENTS

9. REFERENCES

